

Quantum (Inspired) Computing

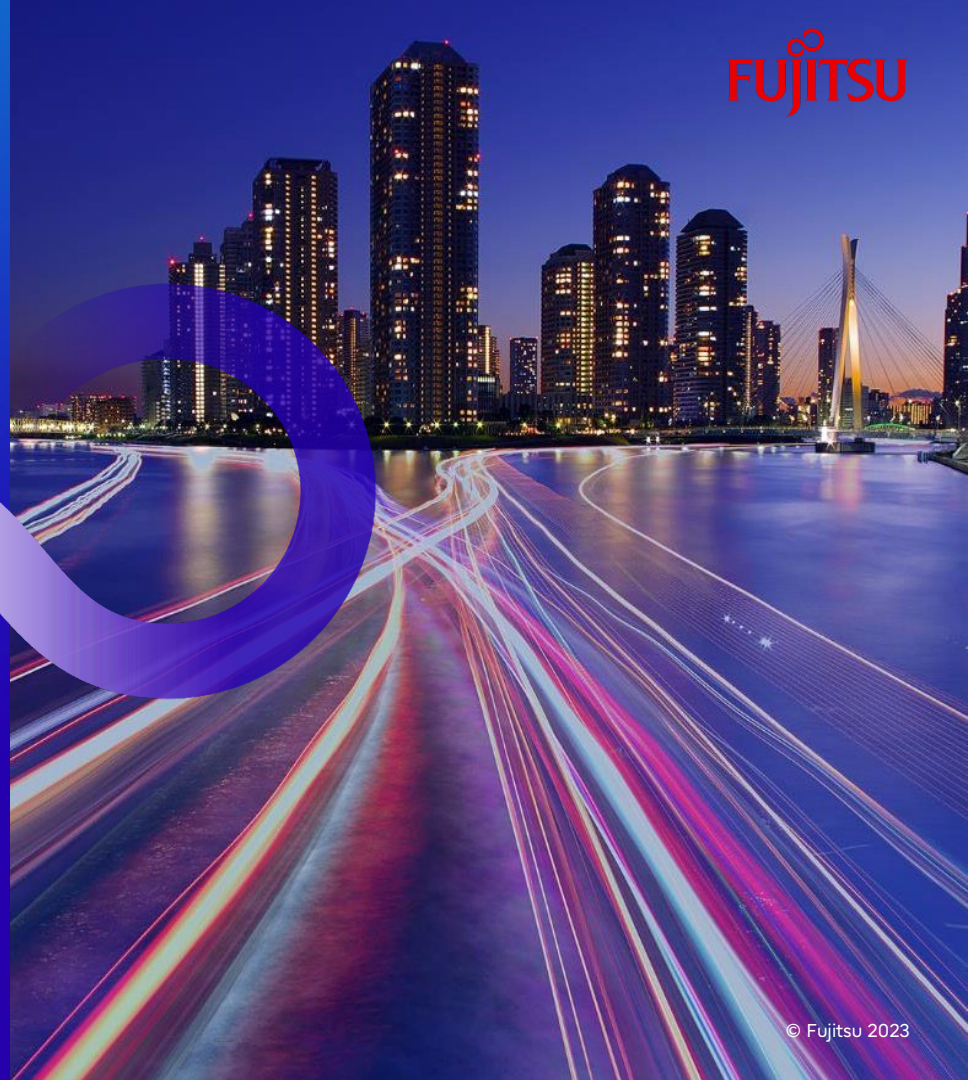
Unlocking value through
solving complex problems

Name

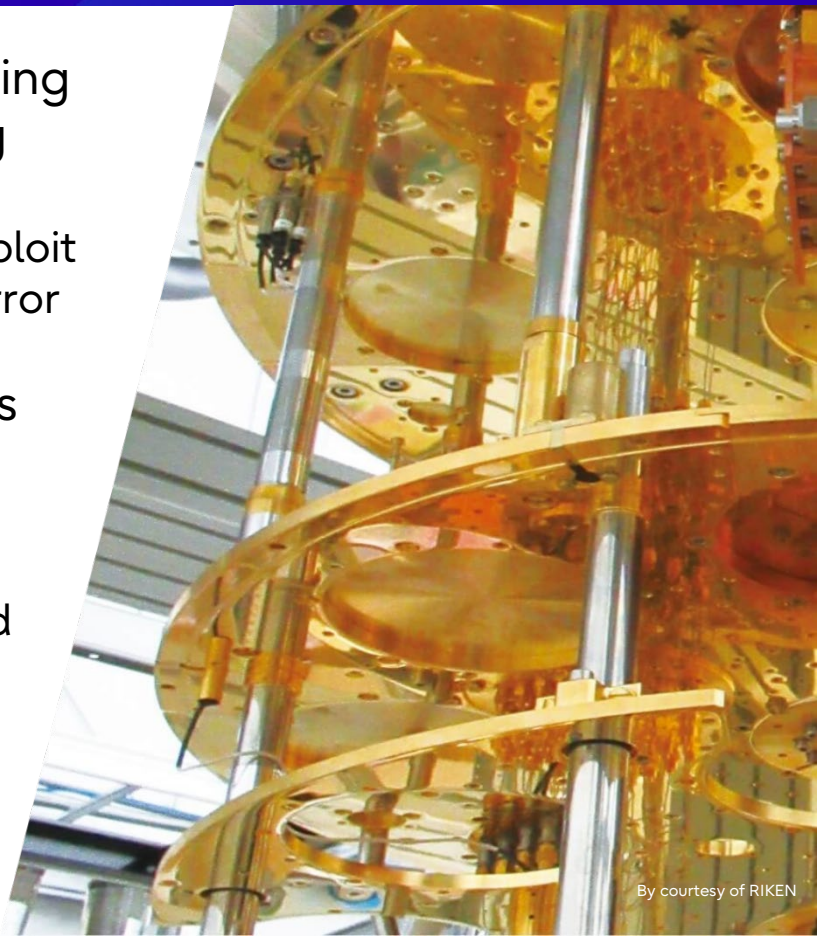
Title

Fujitsu Company

FUJITSU-RESTRICTED



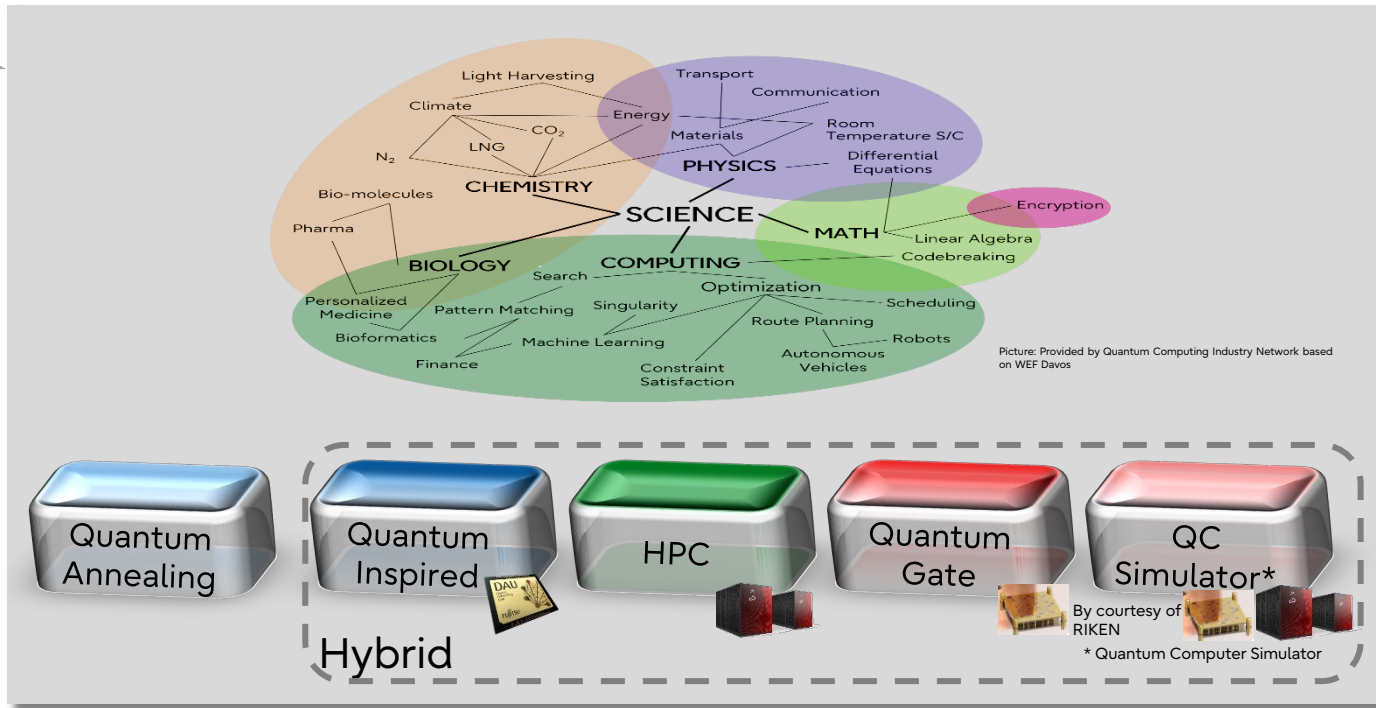
- Quantum Computing holds promise for solving the most complex challenges and unlocking new business advantage
 - **BUT** it will last years or decades until it will exploit its full potential (number of qubits required, error correction, ...)
- **Fujitsu's** approach to Quantum Computing is three prong
 - **Quantum-Inspired**: Solve large, industry-relevant optimization challenges **today**
 - **Quantum Computer Simulator**: Search for and **start** development of quantum algorithms
 - **Quantum Gate**: **Develop** Superconducting Quantum Gate Computer for **hybrid** quantum computing



Unlocking Value from Quantum (Inspired) Computing

Value Assessment, integration into business processes, ...

Business Problem-led

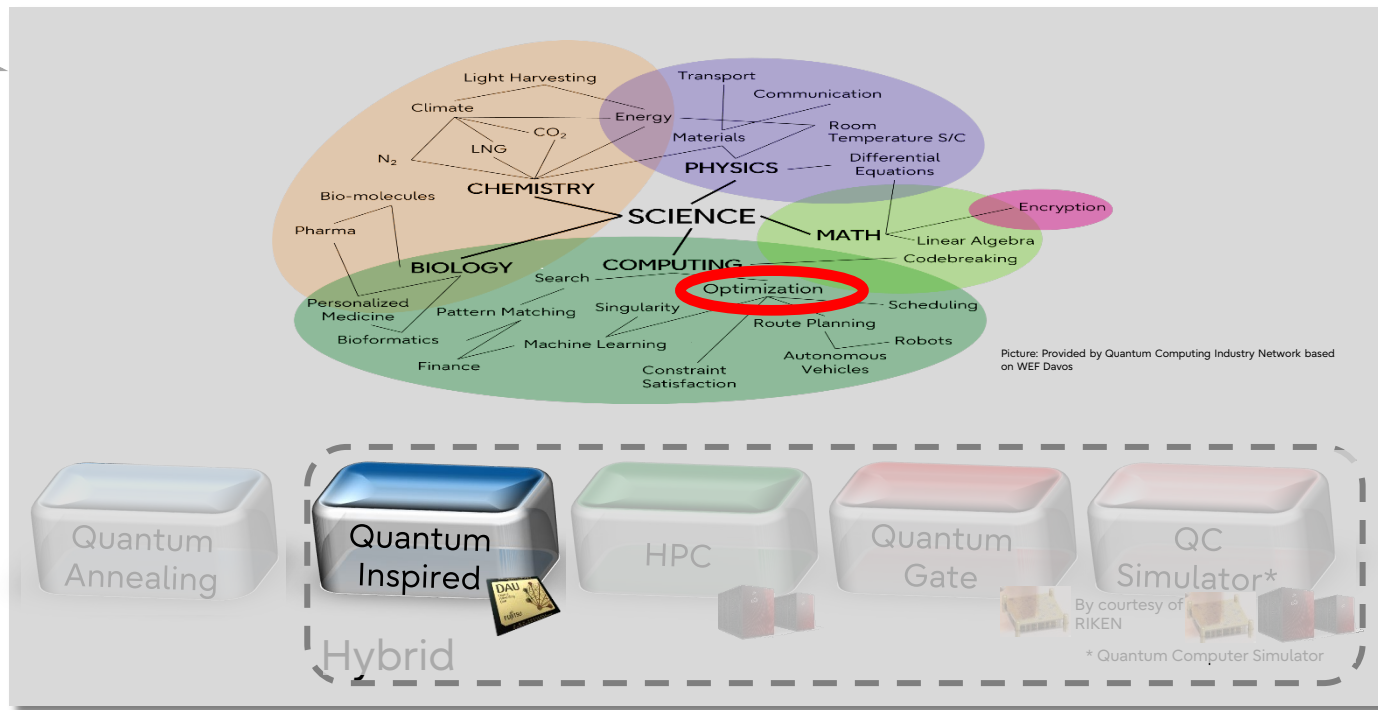


Technology-led

Fidelity, error correction, number of qubits, ...

Unlocking Value from Quantum (Inspired) Computing

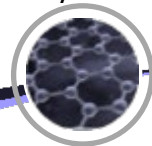
Business Problem-led



Quantum Inspired: The use of computational methods inspired by the principles of quantum mechanics

Digital Annealer - An **available** future-proof on-ramp to Quantum Computing for solving **real-world** combinatorial optimization problems **today**

*Quantum
Computer*



Non-Quantum heritage

- Room temperature
- Classical circuits

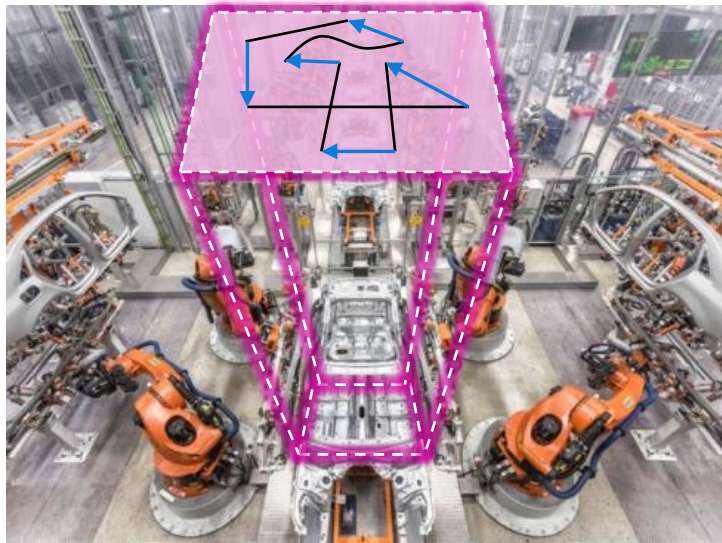
CPU / GPU



Quantum-Inspired

- Inspired by Quantum Entanglement
 - Full-connectivity of all bits
- Inspired by Quantum Superposition
 - Massive parallelism, testing of up to 100,000 bit flips simultaneously
- Inspired by Quantum Tunneling
 - Fast escape from local minima

Example: Welding robots optimization



Find best welding directions and optimal roundtrip between endpoints

# seams	10	65
Possibilities	1.86×10^8	2.34×10^{108}

Typical problem characteristics

- Decisions being made are natively binary ("yes" or "no")
 - Does this robot perform this task at that time?
- The fitness of one decision depends on the state of other decisions
 - Is robot 1 in the working area of robot 2?
- The problem is difficult to solve
 - Huge number of possibilities / dependencies

Where Digital Annealer scores best

- Real time demands
- Solution quality demands
- Problems of higher order (quadratic)

Optimization problems are ubiquitous

- 2/3 of QUTAC use cases can be formulated as QUBO or QAOA

Quantum-Inspired Optimization Projects (Excerpt)

	Hamburg Port Authority	United States Army Analytics Group	Deutsche Bahn	Nippon Yusen Kabushiki Kaisha (NYK)
Use Case	Traffic Light Optimization	Logistics Optimization	Real-Time Schedule Optimization	Car Carrier Optimization
Situation	20,000 trucks/day 35 intersections 	10 inventory centers 15 staging centers 500 Demand regions 5 PPE Categories 	70,000 path candidates $10^{20.357}$ possible schedules 	10^{2000} (un)loading patterns 7000 cars, 12 decks 60 car types, 10 ports 
Results	↓ 20% travel time ↓ 9% CO2	↑ 90% improvement	↓ 2h -> 4min compute time ↑ 10% more path request approvals	↓ 4,000h planning time

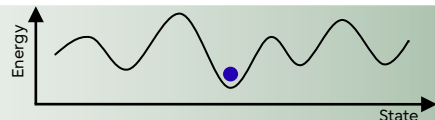
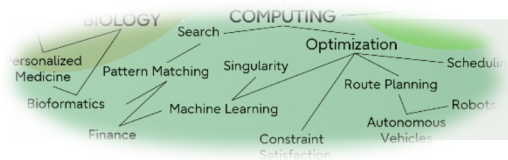
Quantum-Inspired Optimization Projects (Excerpt)

	MediaMarktSaturn Retail Group	Deutsche Telekom	Astroscale	Hospitals
Use Case	Supply Chain Optimization	Automatic Cell Planning	Disposal of Space Debris	Surgery Capacity Optimization
Situation	• 400 stores • 4 vehicle types • Time windows, vehicle capacity, daily travel time / vehicle 	• Site selection problem: An area requires additional sites to improve coverage and service quality 	• Optimize the flight path of spacecrafts for space debris disposal missions 	• Surgeries contribute about 60% of a hospital's total revenue • Hospital Operation Rooms represent major cost centers 
Results	 4,7% delivery costs	 37x compute time  40% quality	 Fuel usage  Efficiency of debris collection.	 Calculations in seconds

Digital Annealer / Quantum Inspired Computing

Technology

Combinatorial Optimization and Quantum



Optimization as search for energy minimum

Any real valued function $E(X)$

$$E(X) = \sum_{i=1}^N b_i x_i + \sum_{i=1}^N \sum_{j=1}^{i-1} w_{ij} x_i x_j$$

Binary Polynomial QUBO

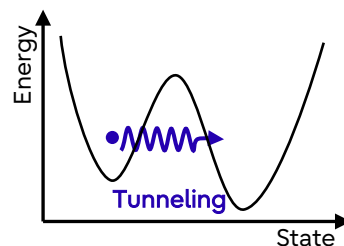
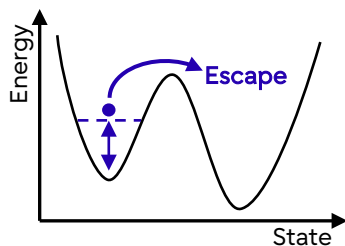
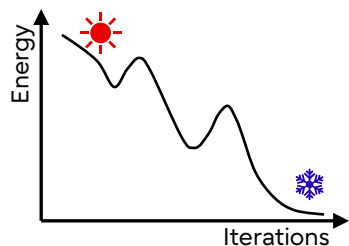
Variational Quantum Algorithm (QAOA)

Simulated Annealing

Digital Annealing

Quantum Annealing

Quantum Gate Computing



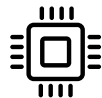
$$\begin{matrix} |0\rangle \\ |0\rangle \end{matrix} \begin{matrix} \boxed{H} \\ \bullet \\ \oplus \end{matrix} \left. \vphantom{\begin{matrix} |0\rangle \\ |0\rangle \end{matrix}} \right\} \frac{1}{\sqrt{2}} [|00\rangle + |11\rangle]$$



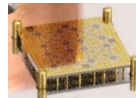
Classical Computer



Digital Annealer



Quantum Annealer



Quantum Gate Computer

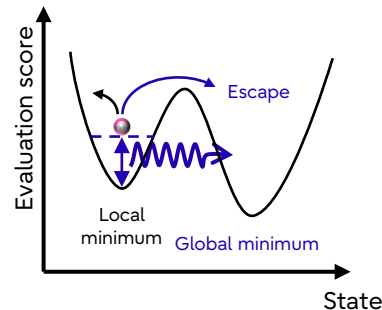
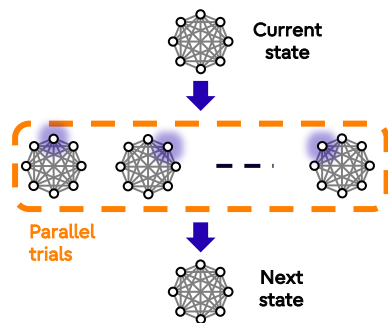
By courtesy of RIKEN

- Special purpose hardware architecture for solving combinatorial **optimization problems**.
- Problem formulation as **QUBO**.
- **Markov Chain Monte Carlo (MCMC)** algorithm as basis to search for minimum of energy function.
- **Speed-Up** due to hardware implementation of MCMC.
 - Parallel search
 - Dynamic offset energy
 - Parallel tempering



$$E(x) = \sum_{i=1}^N b_i x_i + \sum_{i=1}^N \sum_{j=1}^{i-1} w_{ij} x_i x_j \quad x_i \in \{0,1\}$$

$$p(x, x') = \begin{cases} 1 & E(x') \leq E(x) \\ \exp\left(\frac{-(E(x') - E(x))}{T}\right) & E(x') > E(x) \end{cases}$$

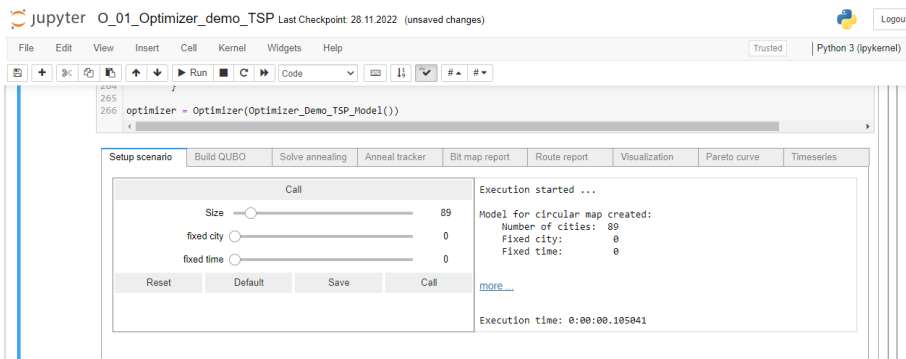




$$E(X) = \sum_{i=1}^N b_i x_i + \sum_{i=1}^N \sum_{j=1}^{i-1} w_{ij} x_i x_j$$
$$X = (x_1, x_2, \dots, x_N) \in \{0, 1\}^N$$
$$b_i \in \mathbb{R}, w_{ij} \in \mathbb{R} \ (i, j = 1, \dots, N)$$

DADK framework

- Create, manipulate, solve QUBOs using DA
- Rapid prototyping
- Load business data
- Visualize results



Get the tutorials

